

#### FOR OFFICIAL USE

National Qualifications 2024

Mark

X847/75/02

Mathematics Paper 2

FRIDAY, 3 MAY 10:30 AM – 12:00 NOON



Fill in these boxes and read what is printed below.

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Day	Month	Year	Scottish c	andidate n	umbe	r				

Total marks — 50

Attempt ALL questions.

You may use a calculator.

To earn full marks you must show your working in your answers.

State the units for your answer where appropriate.

Write your answers clearly in the spaces provided in this booklet. Additional space for answers is provided at the end of this booklet. If you use this space you must clearly identify the question number you are attempting.

Use blue or black ink.

Before leaving the examination room you must give this booklet to the Invigilator; if you do not, you may lose all the marks for this paper.





### **FORMULAE LIST**

The roots of 
$$ax^2 + bx + c = 0 \text{ are } x = \frac{-b \pm \sqrt{(b^2 - 4ac)}}{2a}$$

Sine rule 
$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

Cosine rule 
$$a^2 = b^2 + c^2 - 2bc \cos A \text{ or } \cos A = \frac{b^2 + c^2 - a^2}{2bc}$$

Area of a triangle 
$$A = \frac{1}{2}ab\sin C$$

Volume of a sphere 
$$V = \frac{4}{3}\pi r^3$$

Volume of a cone 
$$V = \frac{1}{3}\pi r^2 h$$

Volume of a pyramid 
$$V = \frac{1}{3}Ah$$

Standard deviation 
$$s=\sqrt{\frac{\Sigma(x-\overline{x})^2}{n-1}}$$
 or 
$$s=\sqrt{\frac{\Sigma x^2-\frac{(\Sigma x)^2}{n}}{n-1}}$$
 , where  $n$  is the sample size.

# Total marks — 50 **Attempt ALL questions**

1. Dougie pays £460 for a new laptop.

It is expected that the value of the laptop will depreciate by 26% each year. Calculate the expected value of Dougie's laptop after 3 years.

3

2. An ant colony occupies an area of 250 hectares.

There is an average of  $1.22 \times 10^6$  ants per hectare.

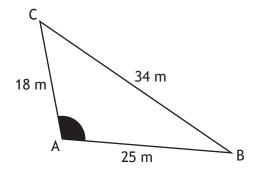
Calculate the number of ants in the colony.

Give your answer in scientific notation.

2



- 3. In triangle ABC:
  - AB = 25 metres
  - AC = 18 metres
  - BC = 34 metres.



Calculate the size of the shaded angle at A.



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4. Solve, algebraically, the inequation

$$5(x-2)+4<7x+8.$$

3

5. This year the cost of Charley's car insurance is £278.40.
This is an increase of 16% on last year's cost.

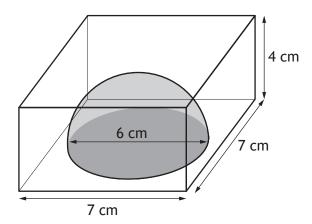
Calculate the cost of Charley's insurance last year.

3

**6.** (a) Factorise  $y^2 - 6y$ .

(b) Hence simplify  $\frac{y^2 - 6y}{y^2 - 3y - 18}$ .

**7.** A paperweight is in the shape of a cuboid. It consists of a hemisphere of red glass surrounded by clear glass.



The cuboid has height 4 centimetres and a square base of length 7 centimetres.

The hemisphere has diameter 6 centimetres.

Calculate the volume of clear glass in the paperweight.

Give your answer correct to 2 significant figures.

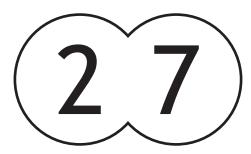
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**8.** Solve the equation  $3x^2 + 8x + 1 = 0$ . Give your answers correct to 2 decimal places.

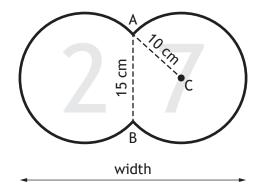
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**9.** Change the subject of the formula  $f = \frac{2d+3}{e}$  to d.

Karen buys a door-number sign for her house. The sign consists of parts of two identical circles.



AB is a chord to both circles.



- AB has length 15 centimetres.
- The radius AC has length 10 centimetres.

Calculate the width of the sign.

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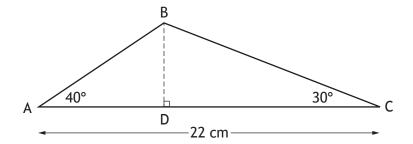
## 12. Express

$$\frac{2}{x+5} + \frac{3}{x-4}, \quad x \neq -5, x \neq 4$$

as a single fraction in its simplest form.

## 13. In triangle ABC:





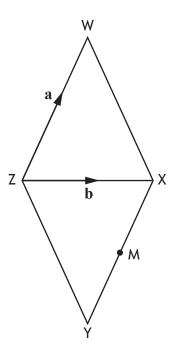
- AC = 22 centimetres
- angle BAC = 40°
- angle BCA = 30°
- BD is perpendicular to AC.

Calculate the length of BD.

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 $\overrightarrow{\mathsf{ZW}}$  represents vector  $\mathbf{a}$  and  $\overrightarrow{\mathsf{ZX}}$  represents vector  $\mathbf{b}$ .

(a) Express  $\overrightarrow{WX}$  in terms of  $\mathbf{a}$  and  $\mathbf{b}$ .

1

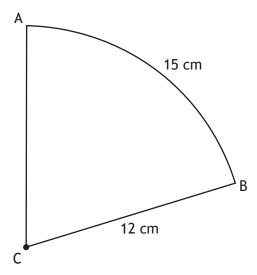
M is the mid-point of XY.

(b) Express  $\overrightarrow{WM}$  in terms of  $\mathbf{a}$  and  $\mathbf{b}$ . Give your answer in its simplest form.



3

### **15.** The diagram shows a sector of a circle, centre C.



The radius of the circle is 12 centimetres.

The length of arc AB is 15 centimetres.

Calculate the area of the sector.



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**16.** Express  $3\cos^2 x^\circ - 1$  in the form  $a + b\sin^2 x^\circ$ . Show your working.

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[END OF QUESTION PAPER]



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### **ADDITIONAL SPACE FOR ANSWERS**



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### **ADDITIONAL SPACE FOR ANSWERS**



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