FOR OFFICIAL USE **National** Qualifications Mark 2014

X747/75/01

TUESDAY, 06 MAY 9:00 AM - 10:00 AM

Mathematics Paper 1 (Non-Calculator)



Fill in these boxes and read what is printed below.

Full name of centre	-	Town	
Forename(s)	Surname		Number of seat
Date of birth Day Month Yea	ar Scottisł	n candidate numbei	r
D D M M Y	Υ		

Total marks — 40

Attempt ALL questions.

Write your answers clearly in the spaces provided in this booklet. Additional space for answers is provided at the end of this booklet. If you use this space you must clearly identify the question number you are attempting.

Use blue or black ink.

You may NOT use a calculator.

Full credit will be given only to solutions which contain appropriate working.

State the units for your answer where appropriate.

Before leaving the examination room you must give this booklet to the Invigilator; if you do not, you may lose all the marks for this paper.





FORMULAE LIST

The roots of
$$ax^2 + bx + c = 0$$
 are $x = \frac{-b \pm \sqrt{(b^2 - 4ac)}}{2a}$

Sine rule:
$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

Cosine rule:
$$a^2 = b^2 + c^2 - 2bc \cos A \text{ or } \cos A = \frac{b^2 + c^2 - a^2}{2bc}$$

Area of a triangle:
$$A = \frac{1}{2}ab\sin C$$

Volume of a sphere:
$$V = \frac{4}{3}\pi r^3$$

Volume of a cone:
$$V = \frac{1}{3}\pi r^2 h$$

Volume of a pyramid:
$$V = \frac{1}{3}Ah$$

Standard deviation:
$$s = \sqrt{\frac{\sum (x - \overline{x})^2}{n - 1}} = \sqrt{\frac{\sum x^2 - (\sum x)^2 / n}{n - 1}}$$
, where n is the sample size.

1. Evaluate $\frac{5}{12} \times 2\frac{2}{9}$.

Give the answer in simplest form.

2

2. Multiply out the brackets and collect like terms:

$$(2x-5)(3x+1)$$
.

2

Page three

Find the resultant vector 2u - v when $u = \begin{pmatrix} -2 \\ 3 \\ 5 \end{pmatrix}$ and $v = \begin{pmatrix} 0 \\ -4 \\ 7 \end{pmatrix}$.

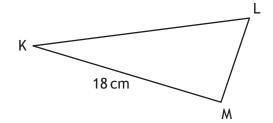
Express your answer in component form.

2

Page four

- KM = 18 centimetres
- sin K = 0·4
- sin L = 0.9

Calculate the length of LM.

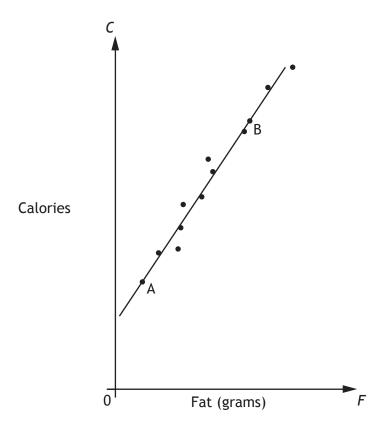


3

Page five

McGregor's Burgers sells fast food.

The graph shows the relationship between the amount of fat, F grams, and the number of calories, C, in some of their sandwiches.



A line of best fit has been drawn.

Point A represents a sandwich which has 5 grams of fat and 200 calories.

Point B represents a sandwich which has 25 grams of fat and 500 calories.

Page six

6. (continued)

MARKS DO NOT WRITE IN THIS MARGIN

(a) Find the equation of the line of best fit in terms of F and C.

3

(b) A Super Deluxe sandwich contains 40 grams of fat.

Use your answer to part (a) to estimate the number of calories this sandwich contains.

Show your working.

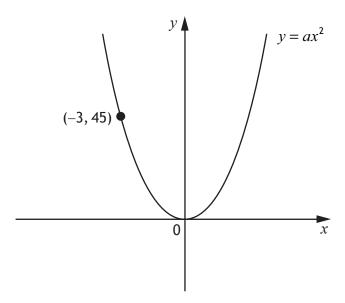
1

Total marks 4



Page seven

The diagram below shows part of the graph of $y = ax^2$



Find the value of a.

2

Page eight

8. Express $\sqrt{40} + 4\sqrt{10} + \sqrt{90}$ as a surd in its simplest form.

9. 480 000 tickets were sold for a tennis tournament last year.

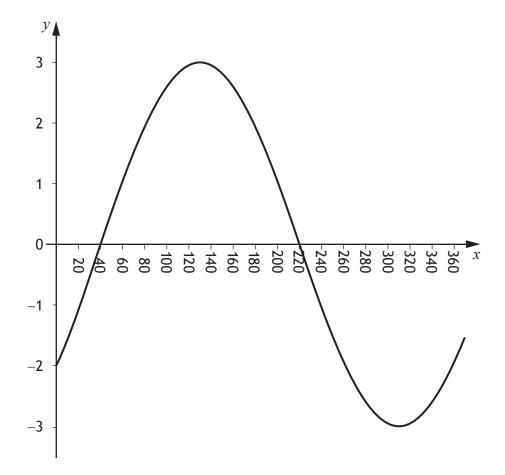
This represents 80% of all the available tickets.

Calculate the total number of tickets that were available for this tournament. 3



Page nine

The graph of $y = a \sin(x+b)^{\circ}$, $0 \le x \le 360$, is shown below.



Write down the values of a and b.

2

Page ten

11. (a) A straight line has equation 4x + 3y = 12. Find the gradient of this line.

2

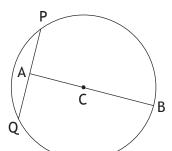
(b) Find the coordinates of the point where this line crosses the x-axis.

2

Total marks 4

Page eleven

12. The diagram below shows a circle, centre C.



The radius of the circle is 15 centimetres.

A is the mid-point of chord PQ.

The length of AB is 27 centimetres.

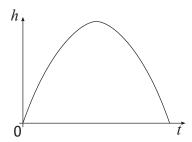
Calculate the length of PQ.

4

MARKS DO NOT WRITE IN THIS MARGIN

The diagram below shows the path of a small rocket which is fired into the air. The height, h metres, of the rocket after t seconds is given by

$$h(t) = 16t - t^2$$



(a) After how many seconds will the rocket first be at a height of 60 metres?

(b) Will the rocket reach a height of 70 metres? Justify your answer.

3

Total marks 7

[END OF QUESTION PAPER]



Page thirteen

ADDITIONAL SPACE FOR ANSWERS

MARKS DO NOT WRITE IN THIS MARGIN

Page fourteen

ADDITIONAL SPACE FOR ANSWERS

MARKS DO NOT WRITE IN THIS MARGIN

Page fifteen

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Page sixteen